A monolithic silicon telescope for hadron beams: numerical and experimental study of the effect of $\Delta E$ detector geometry on microdosimetric distributions

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A monolithic silicon telescope consisting of a surface $\Delta E$ detector 2 µm in thickness coupled to an $E$ detector about 500 µm in thickness made out of a single silicon wafer was recently proposed for the microdosimetric characterization of hadron beams. This work discusses the study of the effect of the geometrical structure of the $\Delta E$ detector on microdosimetric distributions measured by the silicon device in hadron beams. Two different devices, i.e. a single-diode $\Delta E$ detector 1 mm$^2$ in sensitive area and a $\Delta E$ detector geometrically segmented in micrometric cylinders, were irradiated at different phantom depths with 62 AMeV carbon ions in the same experimental conditions. In order to reproduce and deeply analyze the experimental results, a detailed numerical study based on Monte Carlo simulations was carried out through the FLUKA code version 2012, a recent release able to transport heavy ions at energies lower than 100 AMeV (the older lower transport limit) by exploiting the new Boltzman Master Equation model. The comparison between microdosimetric distributions measured by the two different detectors highlighted discrepancies at low lineal energies. Those differences, not reproduced by simulations, are probably due to charge sharing between the $\Delta E$ electrodes and the surrounding guards of the segmented device.

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superconducting cyclotron of the Laboratori Nazionali del Sud - National Institute of Nuclear Physics (INFN-LNS). A picture of the irradiation set-up is shown in Figure 1. The primary beam passes through a 15 μm tantalum foil used for current monitoring and is extracted through a kapton (Ka) window. A collimator, a monitor chamber and a final brass collimator 2.5 cm in diameter are used to shape and monitor the delivered beam. The overall distance between the Ka window and the final collimator is about 140 cm. The depth dose profile of the carbon beam is usually measured with a water phantom through a plane parallel advanced PTW Markus ionization chamber, referred as reference chamber in the following.

The measurements were performed by inserting two different sample detectors in a polymethylmetacrylate (PMMA) phantom at different depths. The two devices differ in the ΔE detector design: i) a standard prototype (MST in the following) with a ΔE stage constituted by a single pad about 1x1 mm² in sensitive area (Figure 2a) and ii) a new device (SMST in the following) having a ΔE stage geometrically segmented in a matrix of 7000 micrometric cylinders (about 9 µm in diameter and about 1.9 µm in height) connected in parallel to give an effective area of about 0.5 mm² (Figure 2b) [6].

3. Experimental results

The MST and the SMST were irradiated across and beyond the Bragg peak, at the positions A-D and E-H of Figure 3, respectively. The aim was to study the response of the detector to carbon ions and to their fragments by acquiring and processing the distributions of the energy \( E_{\Delta E} \) imparted per event in the ΔE stage versus that deposited in the E stage, \( E_E \). The lineal energy spectra were calculated by correcting the energy imparted spectra measured with the silicon ΔE detector for tissue-equivalence and for shape-equivalence, with the procedures described in details in reference [6].

3.1. Measurements across the Bragg peak (points A-D)

Positions A-D in Figure 3 refer to nominal PMMA depths of 7.5, 7.6, 7.65 and 7.7 mm respectively. The lineal energy spectra obtained with the MST and the SMST devices are directly compared in Figures 4a-d. The position of the main peak and the values of the carbon edge agree fairly well. At low y-values the spectra collected by the SMST are characterized by a tail which is populated by about 50% of total events. This contribution may be ascribed to two distinct effects: i) the track length distribution of the cylindrical ΔE elements of the array detector; ii) charge sharing between the ΔE collecting electrodes and their surrounding guards.

3.2. Measurements beyond the primary beam (points E-H): contribution of fragments

Measurement positions E-H in Figure 3 correspond to depths in PMMA of about 8, 9, 12 and 30 mm, respectively. 62 AMeV primary carbon ions do not reach these depths and only fragmentation products are
present. The lineal energy distributions obtained with the MST and the SMST devices at measurement points E-H are shown in Figure 5e-h. The lineal energy threshold resulted to be about 20 keV μm⁻¹. The distributions are characterized by a complex structure due to the presence of different kind of particles at different energies. The contribution of helium ions and protons are located at low y-values (less than 50 keV) owing to their high energy, while boron ion events extend up to 700 keV. This value resulted to be lower than the expected one (i.e. 1000 keV, from stopping-power tables) owing to the use of an averaged correction factor for tissue equivalence correction.

In order to reproduce and deeply analyze the experimental results, in particular to investigate the effects mentioned above, a detailed numerical study based on Monte Carlo simulations was carried out through the FLUKA code version 2012, a recent release able to transport heavy ions at energies lower than 100 AMeV (the older lower transport limit) by exploiting the new Boltzmann Master Equation model.

The geometry of the beam lines used, firstly simulated in details, were simplified with good approximation in order to optimize the computing time. The energy of the primary beam was set to 55.3 AMeV instead of 62 AMeV, to take into account the energy degradation through the beam delivery system and primary carbons were transported in vacuum at the phantom surface. As shown in Figure 6, the depth dose profile obtained with the simplified simulation agrees well with the one measured through the reference chamber.

The energy imparted in the two detector stages at different depths in phantom was calculated on an event-by-event basis by multiple scattering transport.

The lineal energy distributions obtained by simulating the MST and the SMST devices at measurement points 1 and 2 selected for the numerical analysis are shown in Figure 7 together with the corresponding experimental results. In the case of the MST device, results of Monte Carlo simulations agree fairly well with those obtained experimentally. For the SMST, the calculated distributions differ from those measured at low-y values. This disagreement cannot be ascribed to approximations in the simulated geometry or radiation transport, since all parameters were selected to have an accurate calculation. Therefore, the differences between simulated and measured spectra are probably due to events in the experimental distribution which are affected by border effects, in particular by charge sharing between the ΔE electrode and the guard. This effect, negligible when using the MST, becomes important with the SMST, for which the ratio between the area and the perimeter of the ΔE electrode is low.

4. Numerical study with the FLUKA code

In order to reproduce and deeply analyze the experimental results, in particular to investigate the effects mentioned above, a detailed numerical study based on Monte Carlo simulations was carried out.

Figure 6. Depth dose profile measured with the reference chamber (red points) together with that obtained with the FLUKA simulations (black curve). Points 1 and 2 (blue points) refer to the PMMA depths selected for the simulations of the MST device.

Figure 7. Lineal energy spectra measured with the MST (black line) and SMST (red line) at PMMA depths of 7.5 (a), 7.6 (b), 7.65 (c) and 7.7 mm (d) across the Bragg peak.

Figure 5. Lineal energy spectra measured with the MST (black line) and SMST (red line) at PMMA depths of 8 (e), 9 (f), 12 (g) and 30 mm (h), beyond the Bragg peak.
Figure 7. Lineal energy spectra measured (black) and simulated (red) by considering as the detector the SMST (a and b) or the MST (c and d). 1 and 2 are the measurement positions.

Border effects can be clearly observed only in the primary beam (points A-D) because the impinging particles are characterized by a narrow energy distribution peaked at high lineal energy values. Measurements at points E-I do not show differences between MST and SMST since the border effect contribution is spread over the entire spectrum and located mainly at energies below the threshold (see Figure 5).

5. Conclusions

Two monolithic silicon telescopes which differ in the geometrical structure of the ΔE detector were characterized with 62 AMeV carbon ions. Microdosimetric distributions of the hadron beam were measured at different depths within a PMMA phantom.

The analysis of the measured and calculated spectra highlighted a tail on the microdosimetric distributions measured by the segmented monolithic silicon telescope at low lineal energies. Those effects can be associated to charge sharing between the ΔE collecting electrodes and their surrounding guards. Further investigations are needed to better investigate the charge sharing effect on the microdosimetric distributions obtained by the SMST and to identify strategies to minimize its influence. This will be carry out through ion beam analysis technique.

References